Matching

Stephen Pettigrew

April 16, 2014

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Outline



Basics of matching

Balance Metrics

4 Matching in R

- Propensity score and Mahalanobis matching
- Coarsened exact matching
- The sample size-imbalance frontier

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Outline



- Basics of matching
- 3 Balance Metrics
- 4 Matching in R
 - Propensity score and Mahalanobis matching
 - Coarsened exact matching
 - The sample size-imbalance frontier

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Logistics

- Pset and assessment question 7 released tonight.
- You should have submitted your title and abstract for your final paper. Now you should go through and read the abstracts of your classmates and offer them feedback.

As you receive feedback on your abstract, you should update it in your original post.

• Party on Saturday!

Outline



Basics of matching

- Balance Metrics
- 4 Matching in R
 - Propensity score and Mahalanobis matching
 - Coarsened exact matching
 - The sample size-imbalance frontier

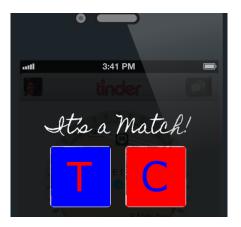
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General Strategy of Matching

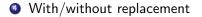
- Determine the variables you want to match on. It's important to match on any potential confounders as well as any imbalanced covariates.
- Choose at matching method (exact, Mahalanobis distance, propensity score, coarsened exact matching, or others).
- Match the treatment and control observations in your data according to the variables and method you chose. Prune any observations that don't have good enough matches.
- Assess the matching procedure by rechecking the balance of your dataset. Iterate through steps 1 through 3 until you're comfortable with the balance in your dataset.
- Use parametric analysis (regress, t-test, etc.) to estimate your treatment effect of interest.
- Perform sensitivity tests to check the assumptions of the matching or modeling procedure.

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Things to think about while matching



- Which distance metric to use
- e How to turn distances into matches
- How to prune the data as you match



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Choosing a distance metric

You want to match together each treatment unit to the control unit (or units) that is most similar to the treatment unit based on pretreatment covariates.

By doing this, you're essentially trying to find control units which can serve as a counterfactual for each treatment unit (and vice versa).

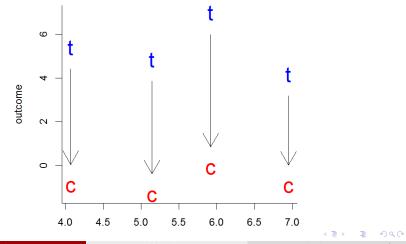
Exact matching

The most straightforward way to do this is by matching each treated unit to a control unit that have *exactly* the same covariate values.

This is called exact matching and can be thought of as the gold-standard for matching.

Exact matching with one covariate

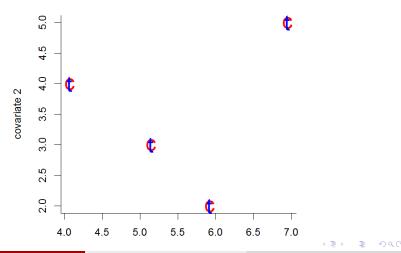
Exact matching with 1 covariate



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April 16, 2014 10 / 66

Exact matching with two covariates



Exact matching with 2 covariates

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Matching

April 16, 2014 11 / 66

Exact matching

When can we not do exact matching?

- When treatment/control units lack a perfect match in the other treatment/control condition (although we could prune these observations)
- More commonly, when you have continuous covariates, since the value of two observations can never be exactly the same

In these cases, we'll need to choose a metric for evaluating distance between units, and then use it to match

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Distance metrics

There's lots of difference ways to measure distance, here are a few:

Exact:

- Distance = 0 if $X_i = X_j$
- Distance = ∞ if $X_i \neq X_j$
- Ideal, but hard for a lot of variables

Mahalanobis:

- Distance $(X_i, X_j) = \sqrt{(X_i X_j)' S^{-1}(X_i X_j)}$, where S^{-1} is the matrix of covariances between the variables
- Doesn't work very well when X is high dimensional because it tries to take into account all interactions between the covariates.
- You can emphasize the importance of a variable by doing Mahalanobis distance matching within calipers

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Distance metrics

Propensity score

- Estimate a logit model where the outcome variable is whether the unit was in treatment or control group
- Estimate $\pi_i \equiv \Pr(T_i = 1|X) = \frac{1}{1 + e^{-X_i\beta}}$

• Distance
$$(X_i, X_j) = |\pi_i - \pi_j|$$

• This overcomes the high-dimensionality problem by summarizing covariates with one number which is interpretable as the probability that the unit was in treatment group

Linear propensity score:

• $\text{Distance}(X_i, X_j) = |\text{logit}(\pi_i) - \text{logit}(\pi_j)|$

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$\mathsf{Distance} \Rightarrow \mathsf{Matches}$

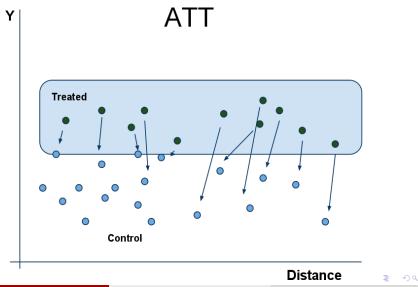
Once we have a distance metric, how do we determine matches?

- 1:1 Nearest neighbor matching
 - Almost always is an estimate of the ATT matches the treated group, then discards the remaining controls.
 - "Greedy": each control unit is only used once
- Optimal matching
 - Instead of being greedy, minimizes a global distance measure
 - Reduces the difference between pairs, but not necessarily the difference between groups

Generally these methods give weights of zero or 1 to observations, depending on whether they are matched.

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Visualizing Nearest Neighbor and Optimal Matches

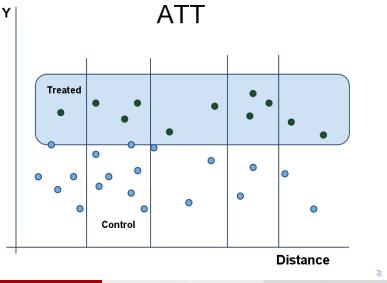


$\mathsf{Distance} \Rightarrow \mathsf{Matches}$

Full matching

- Creates subclasses of variables based on the distance metric
- Estimates the ATT or ATE within each subgroup, weighting each group by the number of observations.
- Weighting based on propensity scores
 - Weighting based on propensity scores is essentially a very fine subclassification scheme
 - To get the ATE, weight by $w_i = \frac{T_i}{\hat{e}_i} + \frac{(1-T_i)}{(1-\hat{e}_i)}$
 - To get the ATT, weight by $w_i = T_i + (1 T_i) rac{\hat{e}_i}{1 \hat{e}_i}$

Visualizing Subclassification



Distance in coarsened exact matching

- CEM is exact matching with coarsening.
- Similar to sub-classification, but the classification is not based on a distance metric, it's based on substantive knowledge of the covariates.
- This allows us to get the benefits of exact matching without the problems of high dimensionality.
- CEM also weights to get the ATT and the ATE depending on how many observations are in the coarsened categories.

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Pros and Cons of 1 to 1 matching

• Cons:

- You are discarding observations
- Might lead to reduced power and bigger standard errors

• Pros:

- You'll tend to get better matches
- It might not lead to reduced power because power is often driven by the size of the smaller group (treated or control).
- Power can be increased if you have better precision (reduced extrapolation)

Alternative to 1 to 1 matching: k-nearest neighbor matching. Match each treated unit to the k control units that are most similar, then average or weight over the potential outcomes of the control units.

Less common in social science, although it's the basis for player evaluation metrics like PECOTA, KUBIAK, and VUKOTA in the sports analytics

world.

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Matching with or without replacement?

Pros of using replacement:

- You will get better matches
- Particularly helpful when you have very few control individuals

• Cons of using replacement:

- More complicated because matched controls are not independent.
- Should be aware of how many times you are using one control.

Outline



Basics of matching

Balance Metrics

Matching in R

- Propensity score and Mahalanobis matching
- Coarsened exact matching
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3

The Goal of Balance

To what extent does the pre-match distribution of X|T = 1 look like the distribution of X|T = 0?

If they are very close, then we have matched well. Example: exact matching leads to identical multivariate distributions:

$$f(X|T = 1) = f(X|T = 0)$$

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Balance tables

Papers that do causal inference or present results of experiments often present a **balance table**

Usually shows summary statistics of covariates separated out by control or treatment groups

Example from Gerber, Green, Larimer (2008):

	Control	Civic Duty	Hawthorne	Self	Neighbors
	Mean	Mean	Mean	Mean	Mean
Household size	1.91	1.91	1.91	1.91	1.91
Nov 2002	.83	.84	.84	.84	.84
Nov 2000	.87	.87	.87	.86	.87
Aug 2004	.42	.42	.42	.42	.42
Aug 2002	.41	.41	.41	.41	.41
Aug 2000	.26	.27	.26	.26	.26
Female	.50	.50	.50	.50	.50
Age (in years)	51.98	51.85	51.87	51.91	52.01
N =	99,999	20,001	20,002	20,000	20,000

Balance tables

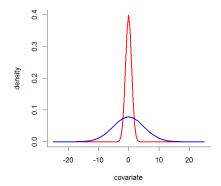
Often balance tables also include information about the variance of the covariates. You can use this information to do a difference in means t-test.

In R:

What does a statistically significant result from this t-test indicate?

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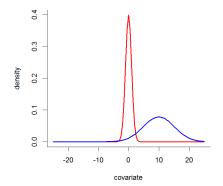
What's wrong with this picture?



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What's wrong with this picture?



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Image: A (□)

This looks balanced, right?

	treatment	control
black	2.00	2.00
white	2.00	2.00
female	2.00	2.00
male	2.00	2.00

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It looks like it's balanced, but it's definitely not:

Treated Units

	female	male
black	2.00	0.00
white	0.00	2.00

Control Units

	female	male
black	0.00	2.00
white	2.00	0.00

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Full dataset

	race	sex	treat
1	black	m	1.00
2	black	m	1.00
3	white	f	1.00
4	white	f	1.00
5	black	f	0.00
6	black	f	0.00
7	white	m	0.00
8	white	m	0.00

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 April 16, 2014
 28 / 66

Multivariate balance: \mathcal{L}_1

The idea is to divide the distributions of X|T = 1 and X|T = 0 each into k bins, sort of like a big multivariate (or univariate) histogram. Bin sizes are usually determined automatically.

We then have a set of frequencies $f_1, ..., f_k$ where f_i is the proportion of treated observations which fall in bin *i*; likewise $g_1, ..., g_k$ are the proportions of control observations falling in bin *i*.

Then

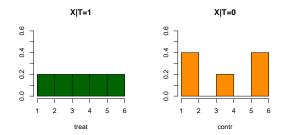
$$\mathcal{L}_1(f,g) = \frac{1}{2} \sum_{i=1,...,k} |f_i - g_i|.$$

If balance is perfect this equals 0; if completely imperfect, 1.

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Multivariate balance: \mathcal{L}_1

Here is a univariate example:



$$L_1(f,g) = \frac{1}{2}(.2 + .2 + 0 + .2 + .2) = .4.$$

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April 16, 2014 30 / 66

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Introducing the Data

Famous LaLonde dataset: an evaluation of a job training program administered in 1976. The data contain a few hundred observations which were part of a randomized experiment, as well as several thousand (non-randomized, control) observations which were drawn from the CPS. Main outcome of interest is re78, retained earnings in 1978; sole treatment is the job training program (treated).

A variety of covariates on which to match:

- age, education (in years), nodegree
- black, hispanic, married
- re74, re75
- u74, u75 both indicators of unemployment

Get the Data

```
install.packages("MatchIt")
install.packages("cem")
library(MatchIt)
library(cem)
library(Zelig)
```

LOAD DATA: Lalonde (1986) dataset; from cem package
data(LL)

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Look at the Data Before Matching

Naïve calculation of the average treatment effect:

mean(LL\$re78[LL\$treated == 1]) - mean(LL\$re78[LL\$treated == 0])
[1] 886.3038

Estimation of ATE using regression:

	Estimate	Std. Error	t value	$\Pr(> t)$
(Intercept)	3185.6806	2637.8616	1.21	0.2276
treated	823.6546	468.4621	1.76	0.0791
age	10.2419	37.0664	0.28	0.7824
education	200.5936	180.5211	1.11	0.2669
black	-1419.1896	801.9466	-1.77	0.0772
married	48.5436	652.2012	0.07	0.9407
nodegree	-299.6107	747.9791	-0.40	0.6889
re74	0.1274	0.0753	1.69	0.0909
re75	0.0647	0.0914	0.71	0.4794
hispanic	299.2882	1050.4602	0.28	0.7758
u74	1529.9294	937.8173	1.63	0.1033
u75	-1005.8379	917.0246	-1.10	0.2731

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Checking Imbalance in R

The most straightforward way to check univariate imbalance is to perform a t-test on the difference in for the covariate of interest between the treatment and control groups.

```
test <- t.test(LL$age[LL$treat == 1], LL$age[LL$treat == 0])</pre>
```

Welch Two Sample t-test

data: LL\$age[LL\$treat == 1] and LL\$age[LL\$treat == 0] t = 0.3565, df = 631.223, p-value = 0.7216 alternative hypothesis: true difference in means is not equal to 0 95 percent confidence interval: -0.807995 1.166403 sample estimates: mean of x mean of y 24.62626 24.44706

Checking Imbalance in R

Multivariate Imbalance Measure: L1=0.735 Percentage of local common support: LCS=12.4%

Univariate Imbalance Measures:

statistic type L1 min 25% 50% 1.792038e-01 (diff) 4.705882e-03 0.00000 0 1 age education 1.922361e-01 (diff) 9.811844e-02 1 0 1.00000 1.070311e-02 (diff) 1.070311e-02 0.00000 married 0 0 . . . re74 -1.014862e+02 (diff) 5.551115e-17 0 0 69.73096 3.941545e+01 (diff) 5.551115e-17 re75 0 0 294.18457 . . .

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Exact Matching

```
exact.match <- matchit(formula= treated ~ age + education
    + black + married + nodegree + re74 + re75 + hispanic +
    u74 + u75, data = LL, method = "exact")</pre>
```

```
Call:
matchit(formula = treated ~ age + education + black + married +
    nodegree + re74 + re75 + hispanic + u74 + u75, data = LL,
    method = "exact")
```

Exact Subclasses: 36

Sample sizes: Control Treated All 425 297 Matched 74 55 Unmatched 351 242

Exact Matching

Look at the matched dataset:

```
exact.data <- match.data(exact.match)</pre>
```

head(exact.data) u74 u75 weights subclass 16110 1 1 1.0000000 1 16141 1 1 1.0000000 2 ... 16148 1 1 1.0000000 3 1 1 0.6727273 3 16156 16164 1 1 1.0000000 4 16182 1 1 4.0363636 14

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What is the Treatment Effect?

Using regression:

Selected output:

Coefficients: Estimate Std. Error t value Pr(>|t|) (Intercept) 3951.7 670.1 5.897 3.14e-08 *** treated 1306.1 1026.2 1.273 0.205

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What is the Treatment Effect?

Using the formula estimator for the ATE:

```
y.treat - y.cont
[1] 1306.075
```

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- 4

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Propensity score matching

The idea with propensity score matching is that we use a logit model to estimate the probability that each observation in our dataset was in the treatment or control group.

Then we use the predicted probabilities to prune out dataset such that, for every treated unit, there's a control unit that can serve as a viable counterfactual.

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Pruning based on propensity scores

Control units>>> 300 200 100 0 100 <<<Treated units 200 300 400 _ 0.1 0.2 0.3 0.5 0.7 0.8 0.9 0 0.4 0.6 Probability of being treated

What to prune with propensity score matching

Stephen Pettigrew

Calculating propensity scores

The model:

$$T_i \sim Bern(\pi_i)$$

 $\pi_i = rac{1}{1 + e^{-X_i\beta}}$

Estimate our coefficients using glm() or zelig():

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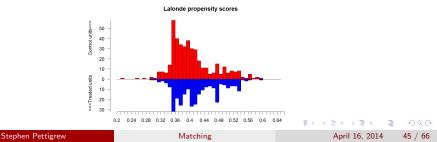
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Calculating propensity scores

Get the propensity score for each observation, which are the same as the predicted probabilities, π_i :

```
fittedvalues <- pscores.logit$fitted
pscore.treat <- fittedvalues[LL$treated == 1]
pscore.control <- fittedvalues[LL$treated == 0]</pre>
```

Determine what observations should be pruned by comparing the overlap in the propensity scores for the treated and control groups:



So far we've looked at how you can use propensity scores to prune your data, but we haven't looked at matching using propensity scores.

Let's return go back to looking at the full dataset and see how to do that

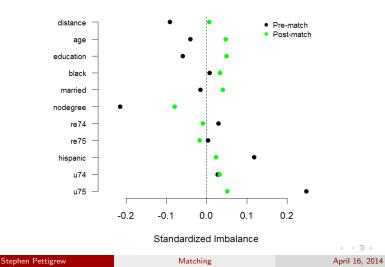
Nearest neighbor matching with propensity scores

Check balance post-matching:

OR

```
pre.balance <- summary(nearest.match)$sum.all
post.balance <- summary(nearest.match)$sum.match</pre>
```

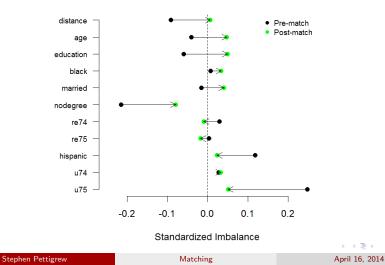
Balance checking



48 / 66

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Balance checking



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48 / 66

Estimating the ATT

nearest.data <- match.data(nearest.match)</pre>

non-parametric estimate of the ATT
mean(nearest.data\$re78[nearest.data\$treated == 1]) mean(nearest.data\$re78[nearest.data\$treated == 0])
[1] 1042.897

A model-based estimate of the ATT
nearest.model <- lm(re78 ~ treated + age + education + black
+ married + nodegree + re74 + re75 + hispanic + u74 + u75,
data = nearest.data)</pre>

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Mahalanobis Matching

Implemented in exactly the same way as propensity score matching in R, except you'll use the distance = ``mahalanobis'' option when you run matchit()

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Outline



Basics of matching

Balance Metrics

4 Matching in R

- Propensity score and Mahalanobis matching
- Coarsened exact matching
- The sample size-imbalance frontier

Stephen Pettig

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CEM: Automatic Coarsening

```
auto.match <- matchit(formula = treated ~ age + education
  + black + married + nodegree + re74 + re75 + hispanic +
  u74 + u75, data = LL, method = "cem")
```

```
Call:
matchit(formula = treated ~ age + education + black + married +
    nodegree + re74 + re75 + hispanic + u74 + u75, data = LL,
   method = "cem")
```

```
Sample sizes:
         Control Treated
A11
            425
                    297
Matched
            222 163
Unmatched
            203 134
Discarded
              Ω
                     0
```

CEM: User Coarsening

```
re74cut <- seq(0, 40000, 5000)
re75cut <- seq(0, max(LL$re75)+1000, by=1000)
agecut <- c(20.5, 25.5, 30.5,35.5,40.5)</pre>
```

```
my.cutpoints <- list(re75=re75cut, re74=re74cut, age=agecut)</pre>
```

CEM: User Coarsening

```
user.data <- match.data(user.match)
auto.data <- match.data(auto.match)
```

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Balance checking

auto.imb\$L1

Multivariate Imbalance Measure: L1=0.592 Percentage of local common support: LCS=25.2%

user.imb\$L1

Multivariate Imbalance Measure: L1=0.437 Percentage of local common support: LCS=43.1%

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CEM: Compare the Two

<pre>summary(auto.match)\$nn</pre>			
	Control Treated		
All	425	297	
Matched	222	163	
Unmatched	203	134	
Discarded	0	0	

<pre>summary(user.match)\$nn</pre>			
Control Treated			
All	425	297	
Matched	182	136	
Unmatched	243	161	
Discarded	0	0	

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CEM: Causal Effects

G0 G1 All 425 297 Matched 182 136 Unmatched 243 161

Linear regression model on CEM matched data:

```
SATT point estimate: 448.556610 (p.value=0.447836)
95% conf. interval: [-708.263075, 1605.376295]
```

CEM: Causal Effects with a Model

	GO	G1
All	425	297
Matched	182	136
Unmatched	243	161

Linear regression model on CEM matched data:

SATT point estimate: 474.936852 (p.value=0.423551) 95% conf. interval: [-686.678239, 1636.551944]

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Outline



Basics of matching

Balance Metrics

Matching in R

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- Propensity score and Mahalanobis matching
- Coarsened exact matching
- The sample size-imbalance frontier

Stephen	Pettigrew
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Intuition behind the frontier



When you prune data by matching, sample size and imbalance trade off with each other

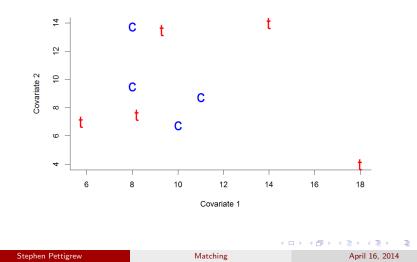
If you don't prune anything, you'll have a big sample size (allowing for better precision) but your data is likely to be very imbalanced

If you prune everything, you'll have perfect balance but you'll have zero observations left to calculate your effects

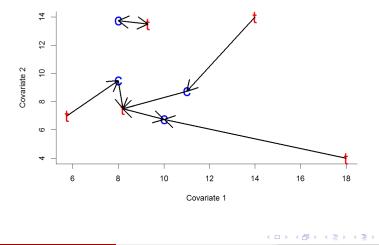
King, Lucas, and Nielsen (2014) provide a way to understand and visualize all the possible matched datasets between these two extremes $r \in \mathbb{R}$ and $r \in \mathbb{R}$ and $r \in \mathbb{R}$

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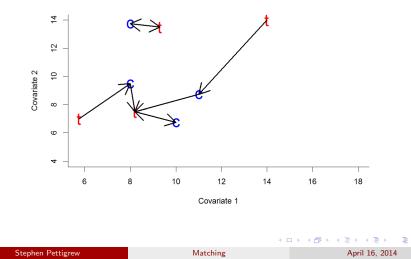
60 / 66



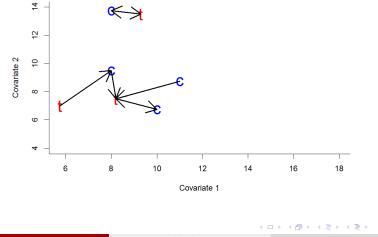
61 / 66



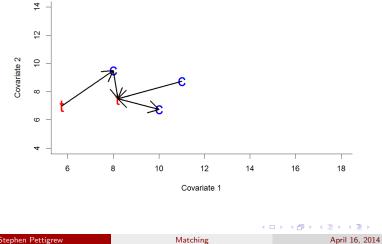
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61 / 66

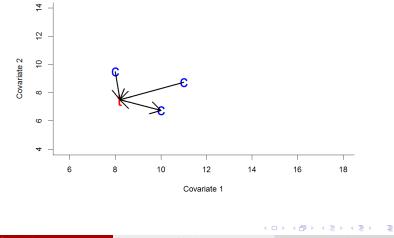


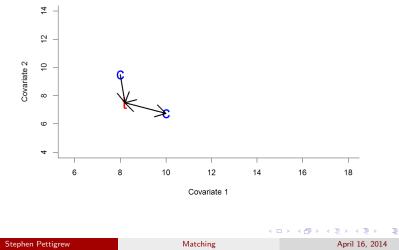
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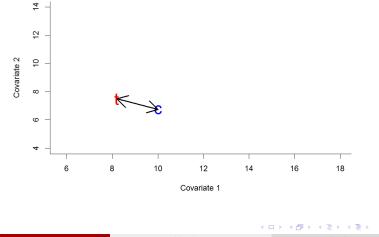
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61 / 66





61 / 66



April 16, 2014 61 / 66

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Installing the MatchingFrontier package

You can find all the documentation and information about the package at: http://projects.iq.harvard.edu/frontier

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Calculating the frontier

The first thing we'll want to do is get a matched dataset for every point along the frontier.

Do this by using the makeFrontier() function:

```
mydataset <- LL
mytreatment <- "treated"
mydrops <- c("treated","re78")</pre>
```

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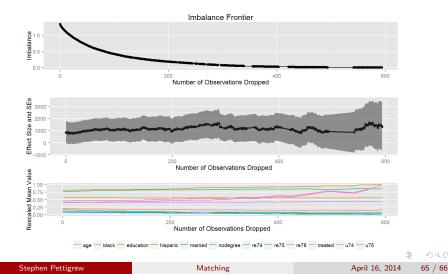
Get the causal effects

You've now got matched datasets for each possible sample size. Let's calculate the FSATT in each one:

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Look at the results

frontierMultiPlot(myfrontier, mydataset, myests)



Questions?

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